

EXERCISES FOR REAL NUMBER ARITHMETIC

Question 1 In Exercises ?? - ??, perform the indicated operations and simplify.

Problem 1.1 $5 - 2 + 3$

6

Problem 1.2 $5 - (2 + 3) = 0$

Problem 1.3 $\frac{2}{3} - \frac{4}{7}$

$\frac{2}{21}$

Problem 1.4 $\frac{3}{8} + \frac{5}{12} = \frac{19}{24}$

Problem 1.5 $\frac{5 - 3}{-2 - 4}$

$-\frac{1}{3}$

Problem 1.6 $\frac{2(-3)}{3 - (-3)} = -1$

Problem 1.7 $\frac{2(3) - (4 - 1)}{2^2 + 1}$

$\frac{3}{5}$

Problem 1.8 $\frac{4 - 5.8}{2 - 2.1} = 18$

Problem 1.9 $\frac{1 - 2(-3)}{5(-3) + 7}$

$-\frac{7}{8}$

Problem 1.10 $\frac{5(3) - 7}{2(3)^2 - 3(3) - 9}$

Undefined. (division by 0.)

Problem 1.11 $\frac{2((-1)^2 - 1)}{((-1)^2 + 1)^2} = 0$

Problem 1.12 $\frac{(-2)^2 - (-2) - 6}{(-2)^2 - 4}$

Undefined. (division by 0.)

Problem 1.13 $\frac{3 - \frac{4}{9}}{-2 - (-3)} = \frac{23}{9}$

Problem 1.14 $\frac{\frac{2}{3} - \frac{4}{5}}{4 - \frac{7}{10}}$

$-\frac{4}{99}$

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$$\text{Problem 1.15} \quad \frac{2 \left(\frac{4}{3}\right)}{1 - \left(\frac{4}{3}\right)^2} = -\frac{24}{7}$$

$$\text{Problem 1.16} \quad \frac{1 - \left(\frac{5}{3}\right) \left(\frac{3}{5}\right)}{1 + \left(\frac{5}{3}\right) \left(\frac{3}{5}\right)}$$

0

$$\text{Problem 1.17} \quad \left(\frac{2}{3}\right)^{-5} = \frac{243}{32}$$

$$\text{Problem 1.18} \quad 3^{-1} - 4^{-2}$$

$$\frac{13}{48}$$

$$\text{Problem 1.19} \quad \frac{1 + 2^{-3}}{3 - 4^{-1}} = \frac{9}{22}$$

$$\text{Problem 1.20} \quad \frac{3 \cdot 5^{100}}{12 \cdot 5^{98}}$$

$$\frac{25}{4}$$

$$\text{Problem 1.21} \quad \sqrt{3^2 + 4^2} = 5$$

$$\text{Problem 1.22} \quad \sqrt{12} - \sqrt{75}$$

$$-3\sqrt{3}$$

$$\text{Problem 1.23} \quad (-8)^{2/3} - 9^{-3/2} = \frac{107}{27}$$

$$\text{Problem 1.24} \quad \left(-\frac{32}{9}\right)^{-3/5}$$

$$-\frac{3\sqrt[5]{3}}{8} = -\frac{3^{6/5}}{8}$$

$$\text{Problem 1.25} \quad \sqrt{(3-4)^2 + (5-2)^2} = \sqrt{10}$$

$$\text{Problem 1.26} \quad \sqrt{(2-(-1))^2 + \left(\frac{1}{2}-3\right)^2}$$

$$\frac{\sqrt{61}}{2}$$

$$\text{Problem 1.27} \quad \sqrt{(\sqrt{5}-2\sqrt{5})^2 + (\sqrt{18}-\sqrt{8})^2} = \sqrt{7}$$

$$\text{Problem 1.28} \quad \frac{-12 + \sqrt{18}}{21}$$

$$\frac{-4 + \sqrt{2}}{7}$$

EXERCISES FOR REAL NUMBER ARITHMETIC

Problem 1.29 $\frac{-2 - \sqrt{(2)^2 - 4(3)(-1)}}{2(3)} = -1$

Problem 1.30 $\frac{-(-4) + \sqrt{(-4)^2 - 4(1)(-1)}}{2(1)}$

$2 + \sqrt{5}$

Problem 1.31 $2(-5)(-5 + 1)^{-1} + (-5)^2(-1)(-5 + 1)^{-2}$
 $\frac{15}{16}$

Problem 1.32 $3\sqrt{2(4) + 1} + 3(4)\left(\frac{1}{2}\right)(2(4) + 1)^{-1/2}(2) = 13$

Problem 1.33 $2(-7)\sqrt[3]{1 - (-7)} + (-7)^2\left(\frac{1}{3}\right)(1 - (-7))^{-2/3}(-1)$
 $-\frac{385}{12}$

Problem 2 With the help of your calculator, find $(3.14 \times 10^{87})^{117}$. Write your final answer, using scientific notation, rounded to two decimal places. (See Example ??.)

1.38×10^{10237}

Problem 3 Prove the Quotient Rule and Power Rule stated in Theorem ??.

Problem 4 Discuss with your classmates how you might attempt to simplify the following.

1. $\sqrt{\frac{1 - \sqrt{2}}{1 + \sqrt{2}}}$

2. $\sqrt[5]{3} - \sqrt[3]{5}$

3. $\frac{\pi + 7}{\pi}$